

## Review for Final Exam

**MULTIPLE CHOICE.** Choose the one alternative that best completes the statement or answers the question.

**Determine whether the relation represents a function. If it is a function, state the domain and range.**

- 1)  $\{(-3, -6), (0, 4), (4, 2), (6, -2)\}$  1) \_\_\_\_\_  
A) function      B) function      C) not a function  
domain:  $\{-6, 4, 2, -2\}$       domain:  $\{-3, 0, 4, 6\}$   
range:  $\{-3, 0, 4, 6\}$       range:  $\{-6, 4, 2, -2\}$

**Find the value for the function.**

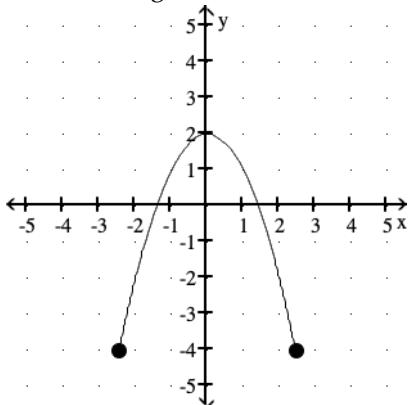
- 2) Find  $f(x + h)$  when  $f(x) = 2x^2 + 4x - 1$ . 2) \_\_\_\_\_  
A)  $2x^2 + 2h^2 + 8x + 8h - 1$   
C)  $2x^2 + 2h^2 + 4x + 4h - 1$   
B)  $2x^2 + 2xh + 2h^2 + 4x + 4h - 1$   
D)  $2x^2 + 4xh + 2h^2 + 4x + 4h - 1$

**Find the domain of the function.**

- 3)  $g(x) = \frac{3x}{x^2 - 9}$  3) \_\_\_\_\_  
A)  $\{x | x > 9\}$   
C) all real numbers  
B)  $\{x | x \neq -3, 3\}$   
D)  $\{x | x \neq 0\}$

**For the function represented in the graph, determine the domain or range, as requested.**

- 4) Find the range. 4) \_\_\_\_\_



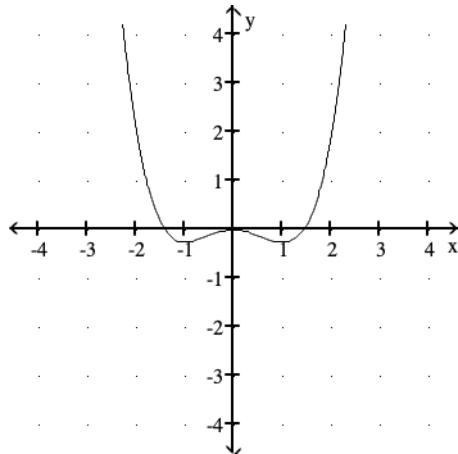
- A)  $[-5, 5]$       B)  $[-2.45, 2.45]$       C)  $[-4, 2]$       D)  $[0, 0]$

**Find the requested value.**

- 5)  $f(4)$  for  $f(x) = \begin{cases} 8x + 1, & \text{if } x < 1 \\ 4x, & \text{if } 4 \leq x \leq 6 \\ 4 - 2x, & \text{if } x > 6 \end{cases}$  5) \_\_\_\_\_  
A) 9      B) 16      C) -4      D) 13

Use the graph of  $f$  to determine the intervals where  $f$  is increasing and where  $f$  is decreasing.

6)

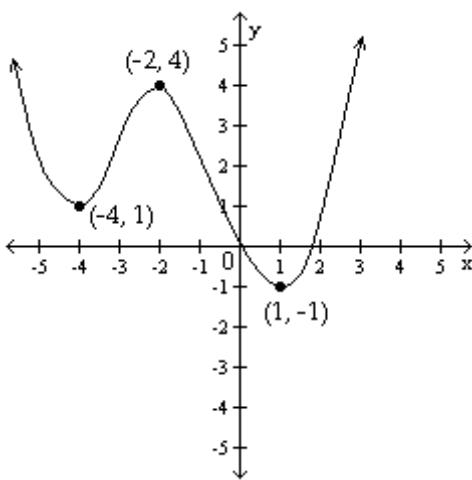


6) \_\_\_\_\_

- A) increasing:  $[-1, 1]$ ; decreasing:  $(-\infty, -1] \cup [1, \infty)$
- B) increasing:  $[-1, 0] \cup [1, \infty)$ ; decreasing:  $(-\infty, -1] \cup [0, 1]$
- C) increasing:  $[0, \infty)$ ; decreasing:  $(-\infty, 0]$
- D) increasing:  $[-1, \infty)$ ; decreasing:  $(-\infty, -1]$

Locate relative maximum and relative minimum points on the graph. State whether each relative extremum point is a turning point.

7)



7) \_\_\_\_\_

- A)  $(-2, 4)$  is a relative maximum point and a turning point.  $(-4, 1)$  and  $(1, -1)$  are relative minima points and turning points.
- B)  $(-2, 4)$  is a relative maximum.  $(-4, 1)$  and  $(1, -1)$  are relative minima points.
- C)  $(-2, 4)$  is a relative maximum and a turning point.  $(-4, 1)$  is a relative minimum point and a turning point.
- D)  $(-2, 4)$  is a relative maximum point and a turning point.  $(1, -1)$  is a relative minimum point and a turning point.

Evaluate.

8) Find  $(f - g)(2)$  when  $f(x) = -5x^2 + 3$  and  $g(x) = x - 5$ .

- A) -24
- B) -10
- C) -14
- D) 15

8) \_\_\_\_\_

- 9) Find  $\left(\frac{f}{g}\right)(-5)$  when  $f(x) = 2x - 7$  and  $g(x) = 2x^2 + 14x + 2$ . 9) \_\_\_\_\_
- A)  $-\frac{1}{9}$       B)  $\frac{17}{18}$       C)  $\frac{2}{3}$       D)  $-\frac{1}{9}$

**For the pair of functions, find the indicated sum, difference, product, or quotient.**

- 10)  $f(x) = 6 - 2x$ ,  $g(x) = -8x^2 + 2$  10) \_\_\_\_\_  
 Find  $(f + g)(x)$ .
- A)  $-10x^2 - 2x + 8$       B)  $-10x + 8$   
 C)  $-8x^2 - 2x + 8$       D)  $-8x^2 + 6$

**For the given functions  $f$  and  $g$ , find the indicated composition.**

- 11)  $f(x) = 4x^2 + 4x + 5$ ,  $g(x) = 4x - 6$  11) \_\_\_\_\_  
 $(g \circ f)(x)$
- A)  $16x^2 + 16x + 14$       B)  $4x^2 + 4x - 1$   
 C)  $16x^2 + 16x + 26$       D)  $4x^2 + 16x + 14$

**Evaluate.**

- 12) Find  $(fg)(-2)$  when  $f(x) = x + 1$  and  $g(x) = 2x^2 + 20x - 7$ . 12) \_\_\_\_\_
- A) 39      B) 43      C) 117      D) -3

**Find the requested function value.**

- 13) Find  $(f \circ g)(-2)$  when  $f(x) = 8x + 3$  and  $g(x) = -5x^2 + 5x + 1$ . 13) \_\_\_\_\_
- A) 11      B) -229      C) 1      D) -909

**Find the requested value.**

- 14) Using the given tables, find  $(f \circ g)(4)$  14) \_\_\_\_\_

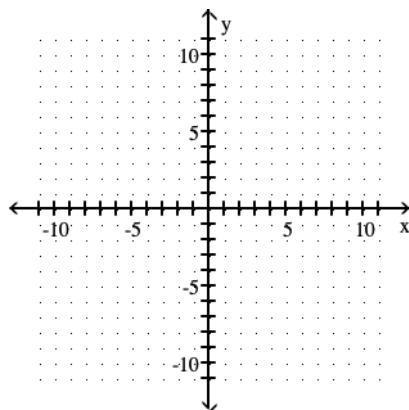
x	13	9	5	7
$f(x)$	26	18	10	14

x	6	4	7	5
$g(x)$	11	7	13	9

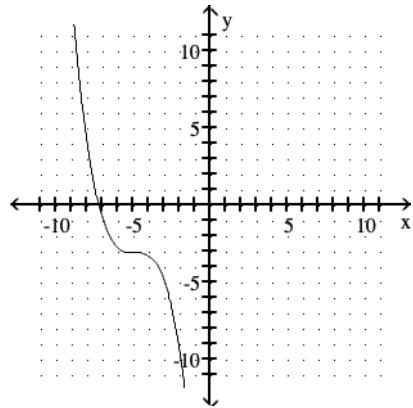
- A) 7      B) 4      C) 18      D) 14

**Graph the function.**

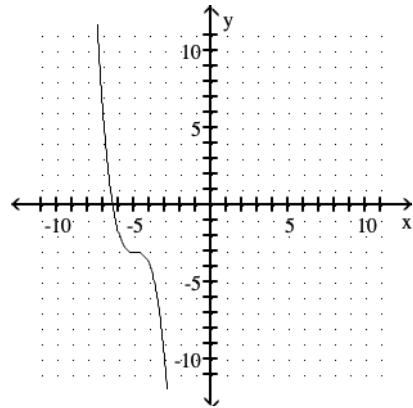
- 15)  $g(x) = -(x + 5)^3 - 3$  15) \_\_\_\_\_



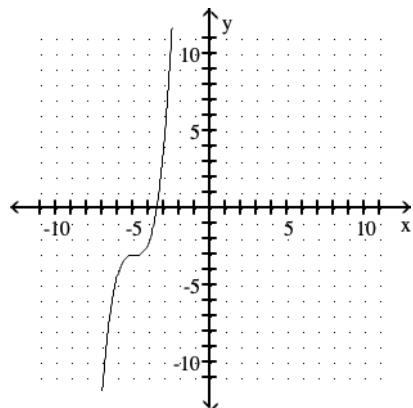
A)



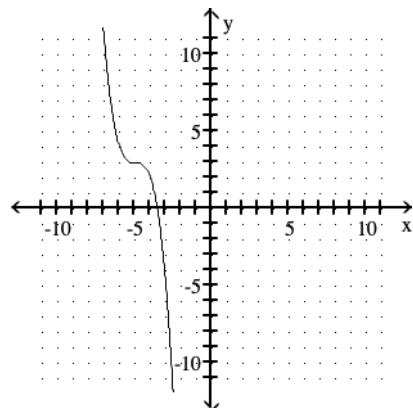
B)



C)

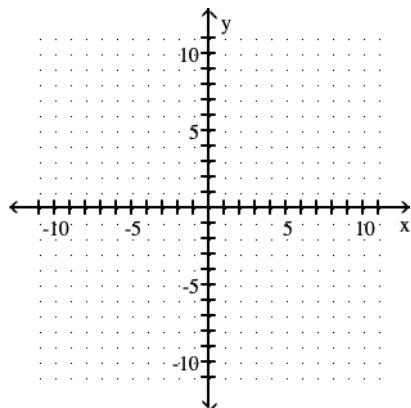


D)

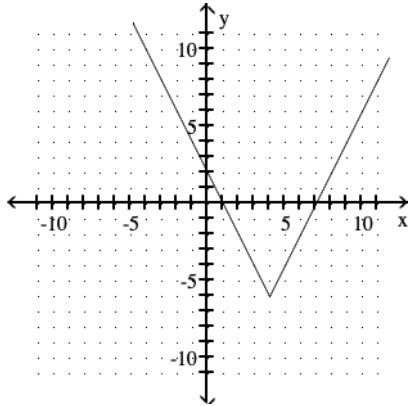


$$16) g(x) = \frac{1}{4}|x - 4| - 6$$

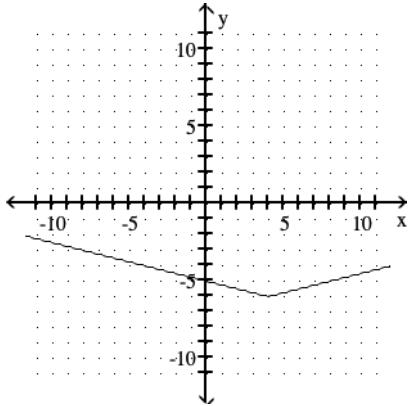
16) \_\_\_\_\_



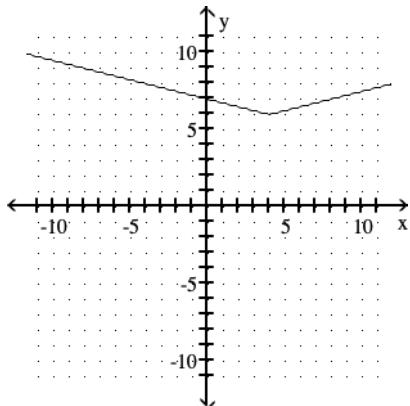
A)



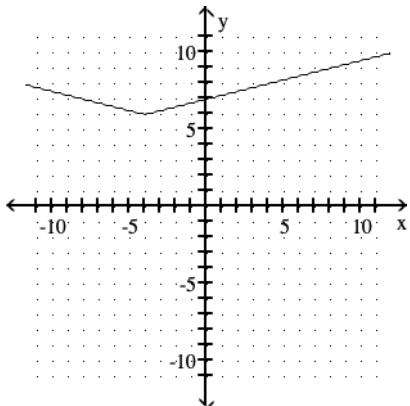
B)



C)

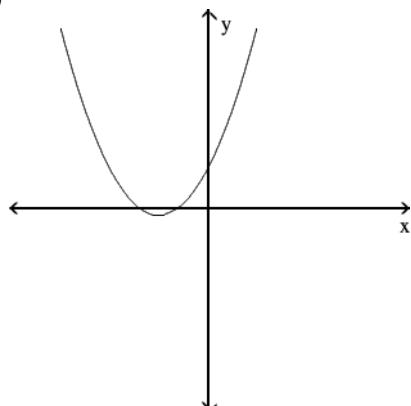


D)



Does the graph represent a function that has an inverse function?

17)



17) \_\_\_\_\_

A) Yes

B) No

Determine whether the given function is one-to-one. If it is one-to-one, find its inverse.

18)  $f(x) = \sqrt[3]{x - 6}$

18) \_\_\_\_\_

A)  $f^{-1}(x) = (x + 6)^3$

B)  $f^{-1}(x) = \sqrt[3]{x - 6}$

C)  $f^{-1}(x) = x^3 + 6$

D)  $f^{-1}(x) = (x - 6)^3$

If the function is one-to-one, find its inverse. If not, write "not one-to-one."

19)  $f(x) = \frac{5}{x-9}$

19) \_\_\_\_\_

A)  $f^{-1}(x) = \frac{-9+5x}{x}$

B) not a one-to-one

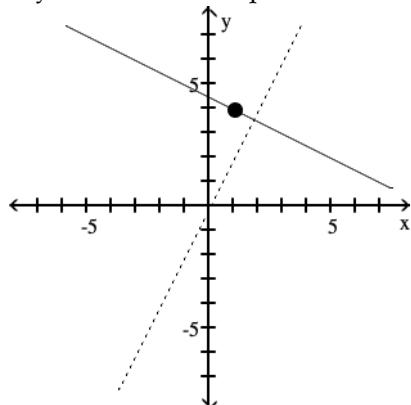
C)  $f^{-1}(x) = \frac{9x+5}{x}$

D)  $f^{-1}(x) = \frac{x}{-9+5x}$

Find an equation for the line with the given properties.

- 20) The solid line L contains the point  $(1, 4)$  and is perpendicular to the dotted line whose equation is  $y = 2x$ . Give the equation of line L in slope-intercept form.

20) \_\_\_\_\_



A)  $y = -\frac{1}{2}x + \frac{9}{2}$

B)  $y - 4 = -\frac{1}{2}(x - 1)$

C)  $y = \frac{1}{2}x + \frac{9}{2}$

D)  $y - 4 = 2(x - 1)$

Write an equation for the linear function and use it to answer the given question.

- 21) You can rent time on computers at the local copy center for a \$7 setup charge and an additional \$ 21) \_\_\_\_\_

4 for every 5 minutes. How much time can you rent for \$17?

A)  $r = 7 - 0.8t$ ; 30 minutes

B)  $r = 7t - 0.8$ ; 2.54 minutes

C)  $r = 7t + 0.8$ ; 2.31 minutes

D)  $r = 7 + 0.8t$ ; 12.5 minutes

Solve the problem.

- 22) Northwest Molded molds plastic handles which cost \$0.10 per handle to mold. The fixed cost to run the molding machine is \$8644 per week. If the company sells the handles for \$4.10 each, how many handles must be molded and sold weekly to break even?

22) \_\_\_\_\_

A) 2058 handles

B) 1440 handles

C) 86,440 handles

D) 2161 handles

Divide and express the result in standard form.

23)  $\frac{6-3i}{5+3i}$

23) \_\_\_\_\_

A)  $\frac{39}{34} - \frac{3}{34}i$

B)  $\frac{21}{34} - \frac{33}{34}i$

C)  $\frac{39}{16} - \frac{33}{16}i$

D)  $\frac{21}{16} - \frac{33}{16}i$

**Solve the equation.**

24)  $x^2 + 4x + 8 = 0$

- A)  $\{-2 - 4i, -2 + 4i\}$   
C)  $\{-2 - 2i, -2 + 2i\}$

- B)  $\{-2 - 2i\}$   
D)  $\{0, -4\}$

24) \_\_\_\_\_

**Find the vertex and axis of symmetry of the graph of the function.**

25)  $f(x) = x^2 + 4x - 5$

- A)  $(-2, 9); x = -2$   
C)  $(2, -9); x = 2$

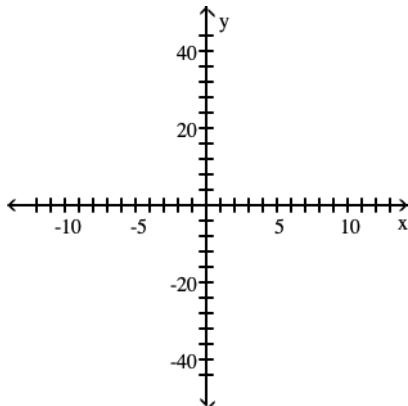
- B)  $(2, 9); x = 2$   
D)  $(-2, -9); x = -2$

25) \_\_\_\_\_

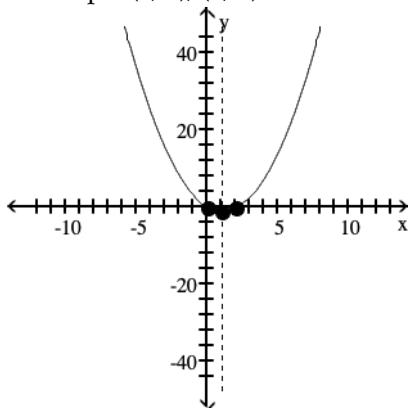
**Graph the function using its vertex, axis of symmetry, and intercepts.**

26)  $f(x) = x^2 - 2x$

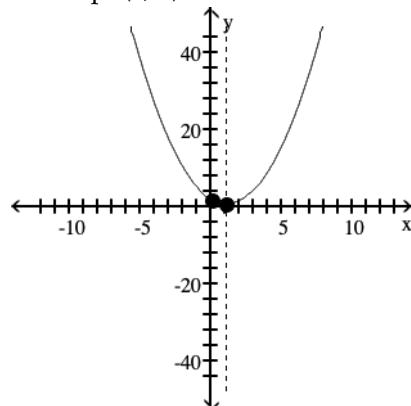
26) \_\_\_\_\_



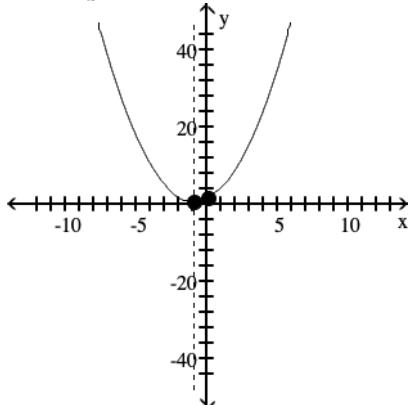
- A) vertex  $(1, -1)$   
intercepts  $(0, 0), (2, 0)$



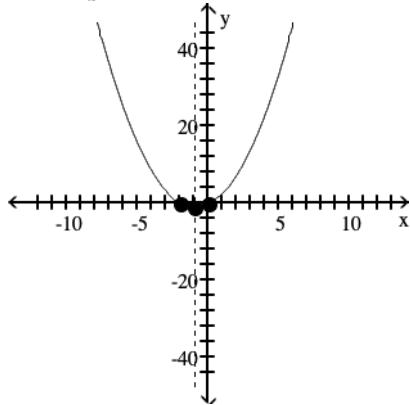
- B) vertex  $(1, 1)$   
intercept  $(0, 2)$



- C) vertex  $(-1, 1)$   
intercept  $(0, 2)$



- D) vertex  $(-1, -1)$   
intercepts  $(0, 0), (-2, 0)$



**Solve the problem.**

- 27) A rock is propelled upward from the top of a building 80 feet tall at an initial velocity of 136 feet per second. The function that describes the height of the rocket in terms of time  $t$  is

$$s(t) = -16t^2 + 136t + 80.$$

Determine the maximum height that the rock reaches.

- A) 331 ft      B) 387 ft      C) 351 ft      D) 369 ft

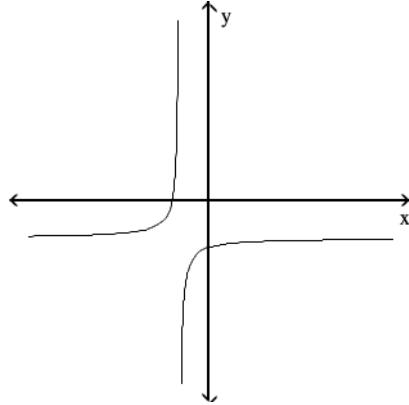
- 28) The owner of a video store has determined that the cost  $C$ , in dollars, of operating the store is approximately given by  $C(x) = 2x^2 - 22x + 760$ , where  $x$  is the number of videos rented daily. Find the lowest cost to the nearest dollar.

- A) \$518      B) \$639      C) \$821      D) \$700

**Determine whether the graph shown is the graph of a polynomial function.**

29)

29) \_\_\_\_\_



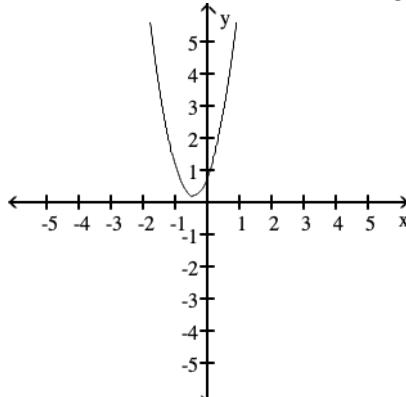
- A) polynomial function

- B) not a polynomial function

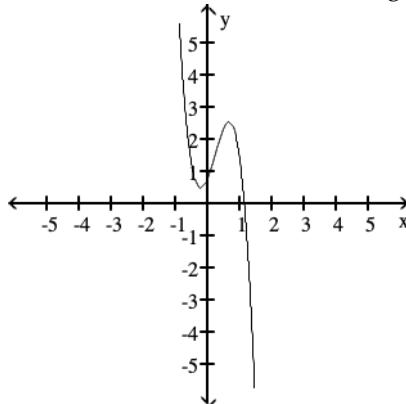
Use the Leading Coefficient Test to determine the end behavior of the polynomial function. Then use this end behavior to match the function with its graph.

30)  $f(x) = -6x^3 + 3x^2 + 3x + 1$

- A) rises to the left and rises to the right

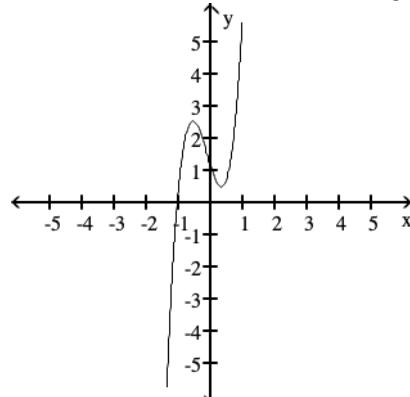


- C) rises to the left and falls to the right

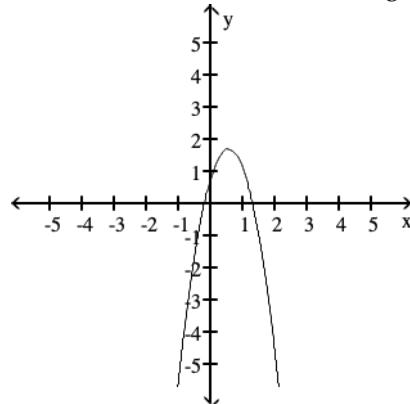


30) \_\_\_\_\_

- B) falls to the left and rises to the right



- D) falls to the left and falls to the right



Divide using long division.

31)  $(-21x^2 + 64x - 35) \div (-7x + 5)$

A)  $3x - 7$

B)  $x - 7$

C)  $-21x - 7$

31) \_\_\_\_\_

D)  $-7x + 1$

Divide using synthetic division.

32)  $(x^2 + 15x + 49) \div (x + 6)$

A)  $x + 10$

B)  $x + 9 - \frac{5}{x+6}$

C)  $\frac{x+9}{x+6}$

D)  $x + 9 + \frac{5}{x+6}$

32) \_\_\_\_\_

Solve the problem.

33) Use synthetic division to divide  $f(x) = x^3 + 11x^2 + 16x - 84$  by  $x + 7$ . Use the result to find all zeros of  $f$ .

33) \_\_\_\_\_

A)  $\{-7, 6, -2\}$

B)  $\{7, -6, 2\}$

C)  $\{-7, -6, 2\}$

D)  $\{7, 6, -2\}$

**Use the Rational Zero Test to list all possible rational zeros for the given function.**

34)  $f(x) = -2x^3 + 4x^2 - 3x + 8$

34) \_\_\_\_\_

A)  $\pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8$

B)  $\pm \frac{1}{8}, \pm \frac{1}{4}, \pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8$

C)  $\pm \frac{1}{4}, \pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8$

D)  $\pm \frac{1}{2}, \pm 1, \pm 2, \pm 4$

**Find the vertical asymptotes, if any, of the graph of the rational function.**

35)  $h(x) = \frac{x+5}{x^2 - 25}$

35) \_\_\_\_\_

A)  $x = 5, x = -5$

B)  $x = 5$

C)  $x = -5$

D) no vertical asymptote

**Find the horizontal asymptote, if any, of the graph of the rational function.**

36)  $g(x) = \frac{7x^2 - 3x - 6}{3x^2 - 8x + 6}$

36) \_\_\_\_\_

A)  $y = 0$

B)  $y = \frac{7}{3}$

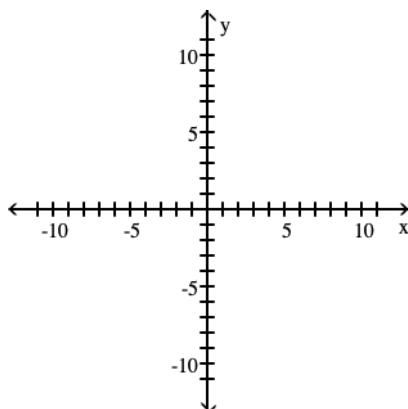
C)  $y = \frac{3}{8}$

D) no horizontal asymptote

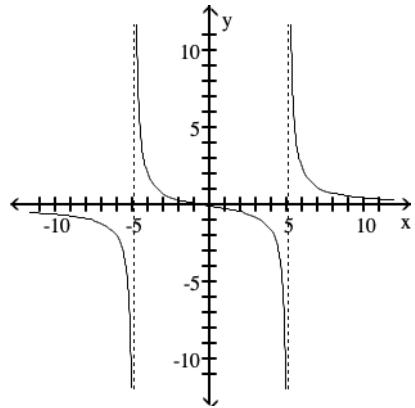
**Graph the rational function.**

37)  $f(x) = \frac{4x^2}{x^2 - 25}$

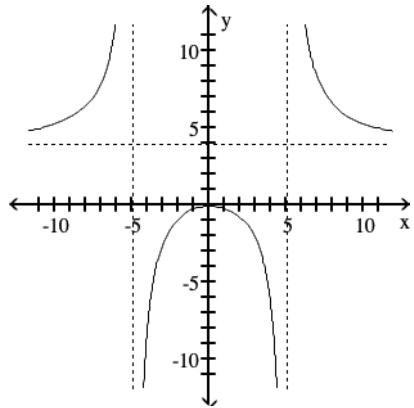
37) \_\_\_\_\_



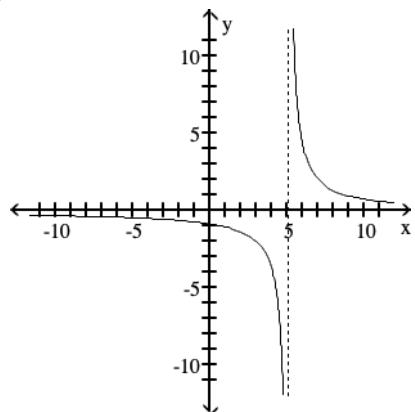
A)



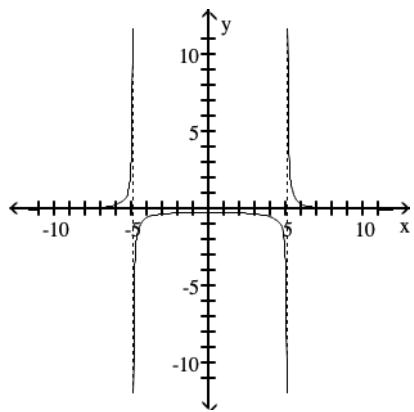
B)



C)

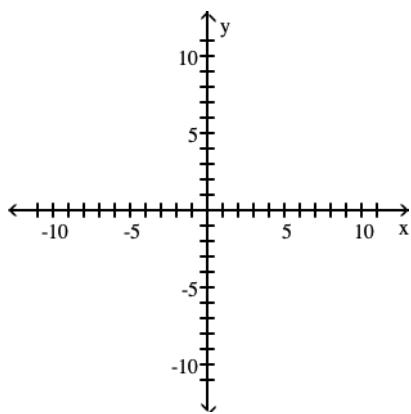


D)

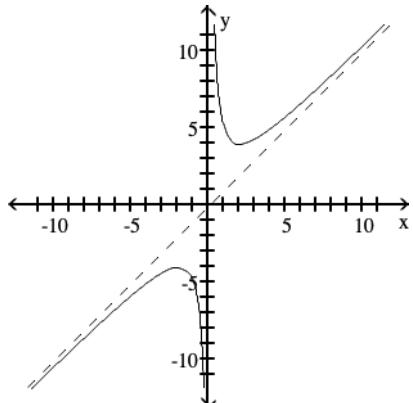
**Graph the function.**

38)  $f(x) = \frac{x^2 - 4}{x}$

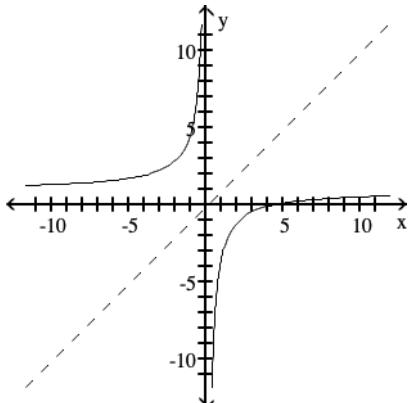
38) \_\_\_\_\_



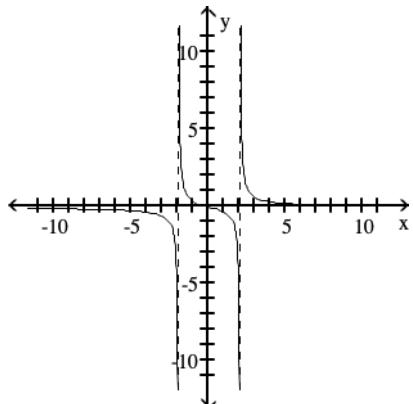
A)



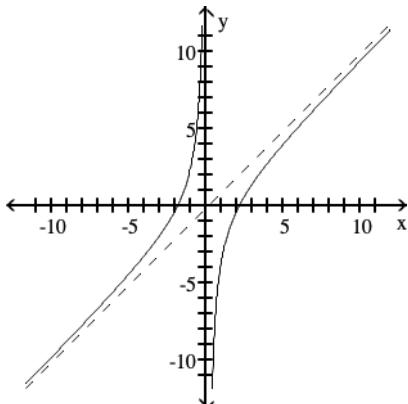
B)



C)



D)



Solve the equation by expressing each side as a power of the same base and then equating exponents.

39)  $9^x + 5 = 27^{x-3}$

A) {8}

B) {19}

C) {13}

D) {14}

39) \_\_\_\_\_

Solve the exponential equation. Use a calculator to obtain a decimal approximation, correct to two decimal places, for the solution.

40)  $3^{(4x-1)} = 19$

A) {0.27}

B) {0.42}

C) {1.83}

D) {0.92}

40) \_\_\_\_\_

Use the compound interest formulas  $A = P \left(1 + \frac{r}{n}\right)^{nt}$  and  $A = Pe^{rt}$  to solve.

41) Find the accumulated value of an investment of \$1500 at 12% compounded quarterly for 2 years.

A) \$1591.35

B) \$1881.60

C) \$1860.00

D) \$1900.16

41) \_\_\_\_\_

42) Find the accumulated value of an investment of \$5000 at 5% compounded monthly for 8 years.

A) \$12,911.25

B) \$8060.16

C) \$9093.60

D) \$7452.93

42) \_\_\_\_\_

43) Find the accumulated value of an investment of \$5000 at 8% compounded continuously for 6 years.

A) \$7400.00

B) \$8180.37

C) \$8080.37

D) \$7934.37

43) \_\_\_\_\_

**Solve the equation.**

44)  $\log_6(x^2 - x) = 1$

44) \_\_\_\_\_

A)  $\{-2, 3\}$

B)  $\{1, 6\}$

C)  $\{2, 3\}$

D)  $\{-2, -3\}$

**Solve the logarithmic equation. Be sure to reject any value that is not in the domain of the original logarithmic expressions. Give the exact answer.**

45)  $\log_2(x + 2) + \log_2(x - 4) = 4$

45) \_\_\_\_\_

A)  $\{-4\}$

B)  $\{7\}$

C)  $\{6\}$

D)  $\{6, -4\}$

46)  $\log_5(x + 2) - \log_5 x = 2$

46) \_\_\_\_\_

A)  $\{5\}$

B)  $\{\frac{2}{25}\}$

C)  $\{12\}$

D)  $\{\frac{1}{12}\}$

**Find a positive angle and a negative angle that are coterminal to the given angle.**

47)  $43^\circ$

47) \_\_\_\_\_

A)  $403^\circ; -137^\circ$

B)  $133^\circ; -47^\circ$

C)  $403^\circ; -317^\circ$

D)  $223^\circ; -137^\circ$

**Convert the angle from degree measure to radian measure. Round to the nearest hundredth of a radian when appropriate.**

48)  $450^\circ$

48) \_\_\_\_\_

A)  $-\frac{5\pi}{4}$

B)  $\frac{5\pi}{2}$

C)  $5\pi$

D)  $-\frac{5\pi}{2}$

**Convert the angle from radian measure to degree measure. Round to the nearest hundredth of a degree when appropriate.**

49)  $\frac{7\pi}{4}$

49) \_\_\_\_\_

A)  $315^\circ$

B)  $102.86\pi^\circ$

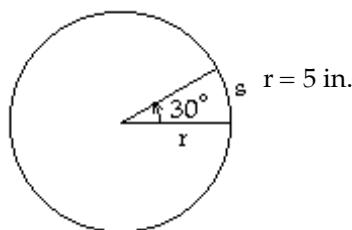
C)  $154.29^\circ$

D)  $630^\circ$

**Solve the problem.**

50) Use the formula  $s = r\theta$  to determine the value of  $s$  in the figure. Round to two decimal places, if necessary.

50) \_\_\_\_\_



A) 0.52 in.

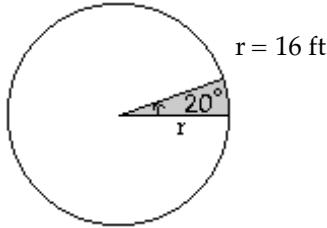
B) 9.55 in.

C) 150 in.

D) 2.62 in.

51) Find the area of the shaded sector. Round to one decimal place.

51) \_\_\_\_\_



A)  $2.8 \text{ ft}^2$

B)  $89.4 \text{ ft}^2$

C)  $44.7 \text{ ft}^2$

D)  $0.5 \text{ ft}^2$

Use the given trigonometric function value of  $\theta$  to find the requested trigonometric function value of the acute angle  $\theta$ . Rationalize the denominator where necessary.

52)  $\cot \theta = \frac{\sqrt{3}}{3}$  Find  $\sin \theta$ .

52) \_\_\_\_\_

A)  $\sqrt{3}$

B)  $\frac{\sqrt{3}}{2}$

C)  $\frac{1}{2}$

D) 2

Rewrite the expression in terms of  $\sin \theta$  and  $\cos \theta$ .

53)  $\tan \theta(\cot \theta - \cos \theta)$

53) \_\_\_\_\_

A) 1

B)  $1 - \sin \theta$

C) 0

D)  $-\sec^2 \theta$

Use a calculator to find the approximate value of the expression. Round the answer to two decimal places.

54)  $\cos \frac{2\pi}{5}$

54) \_\_\_\_\_

A) 1.00

B) 1.07

C) 0.31

D) 0.38

Solve the problem.

55) Find the height of a pine tree that casts a 43-foot shadow on the ground assuming that the angle of elevation from the point on the ground at the tip of the shadow to the sun is  $64^\circ$ . Round your answer to the nearest foot.

55) \_\_\_\_\_

A) 88 ft

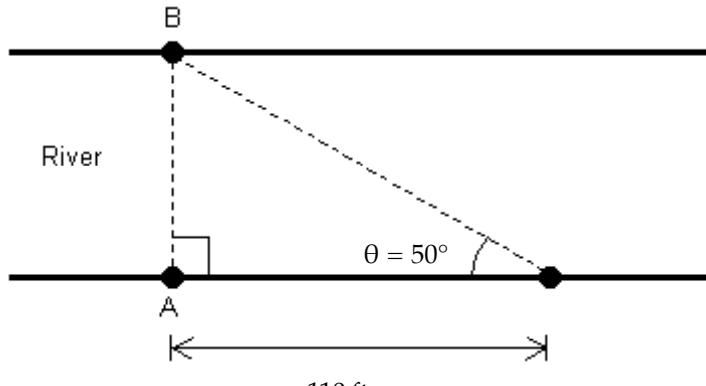
B) 21 ft

C) 39 ft

D) 19 ft

- 56) A conservation officer needs to know the width of a river in order to set instruments correctly for a study of pollutants in the river. From point A, the conservation officer walks 110 feet downstream and sights point B on the opposite bank to determine that  $\theta = 50^\circ$  (see figure). How wide is the river?

56) \_\_\_\_\_



A) 84 ft

B) 171 ft

C) 92 ft

D) 131 ft

**A point on the terminal side of angle  $\theta$  is given. Find the exact value of the indicated trigonometric function.**

57)  $(-2, -3)$  Find  $\sec \theta$ .

57) \_\_\_\_\_

A)  $-\frac{\sqrt{13}}{2}$

B)  $-\frac{2\sqrt{13}}{13}$

C)  $\frac{\sqrt{13}}{3}$

D)  $\frac{3}{2}$

**Name the quadrant in which the angle  $\theta$  lies.**

58)  $\cot \theta < 0, \cos \theta > 0$

58) \_\_\_\_\_

A) I

B) II

C) III

D) IV

**Find the reference angle of the given angle.**

59)  $406^\circ$

59) \_\_\_\_\_

A)  $136^\circ$

B)  $134^\circ$

C)  $46^\circ$

D)  $44^\circ$

**Find the exact value of the indicated trigonometric function of  $\theta$ .**

60)  $\sec \theta = \frac{9}{8}$ ,  $\theta$  in quadrant IV Find  $\tan \theta$ .

60) \_\_\_\_\_

A)  $-\frac{\sqrt{17}}{8}$

B)  $-\sqrt{17}$

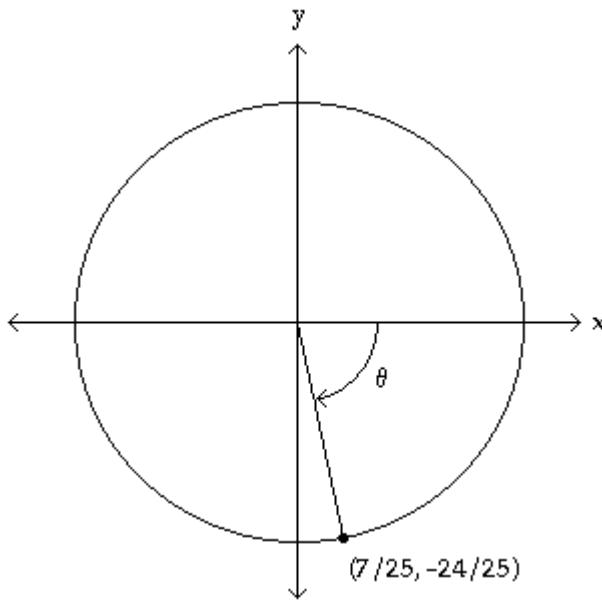
C)  $-\frac{\sqrt{17}}{9}$

D)  $-\frac{9}{8}$

The figure shows angle  $\theta$  in standard position with its terminal side intersecting the unit circle. Evaluate  $\sin \theta$  and  $\cos \theta$ .

61)

61) \_\_\_\_\_



A)  $\sin \theta = -\frac{24}{7}$ ,  $\cos \theta = -\frac{7}{24}$

B)  $\sin \theta = -\frac{25}{24}$ ,  $\cos \theta = \frac{25}{7}$

C)  $\sin \theta = \frac{7}{25}$ ,  $\cos \theta = -\frac{24}{25}$

D)  $\sin \theta = -\frac{24}{25}$ ,  $\cos \theta = \frac{7}{25}$

Find the exact value of the expression.

62)  $\cos^{-1} \frac{\sqrt{3}}{2}$

62) \_\_\_\_\_

A)  $\frac{11\pi}{6}$

B)  $\frac{7\pi}{4}$

C)  $\frac{\pi}{6}$

D)  $\frac{\pi}{4}$

Use a calculator to find the value of the expression rounded to two decimal places.

63)  $\tan^{-1} (-2.2)$

63) \_\_\_\_\_

A) -65.56

B) -24.44

C) -0.43

D) -1.14

Express the given quantity in terms of  $\sin x$  or  $\cos x$ .

64)  $\sin (4\pi - x)$

64) \_\_\_\_\_

A)  $\sin (-x)$

B)  $-\sin x$

C)  $\cos x - \sin x$

D)  $\sin x$

65)  $\cos (4\pi + x)$

65) \_\_\_\_\_

A)  $-\cos x$

B)  $-\sin x$

C)  $\cos x$

D)  $\cos x - \sin x$

**Use the given information to find the exact value.**

66)  $\cos A = \frac{1}{3}$ ,  $0 < A < \frac{\pi}{2}$ ;  $\sin B = -\frac{1}{2}$ ,  $\frac{3\pi}{2} < B < 2\pi$  Find  $\sin(A - B)$ . 66) \_\_\_\_\_

A)  $\frac{\sqrt{3} - 2\sqrt{2}}{6}$

B)  $\frac{\sqrt{3} + 2\sqrt{2}}{6}$

C)  $\frac{2\sqrt{6} + 1}{6}$

D)  $\frac{2\sqrt{6} - 1}{6}$

**Use the information given about the angle  $\theta$ , to find the exact value of the indicated trigonometric function.**

67)  $\sin \theta = -\frac{4}{5}$ ,  $\theta$  in quadrant IV Find  $\sin 2\theta$ . 67) \_\_\_\_\_

A)  $-\frac{7}{25}$

B)  $\frac{24}{25}$

C)  $-\frac{24}{25}$

D)  $\frac{7}{25}$

**Find the exact value by using a half-angle identity.**

68)  $\cos 22.5^\circ$  68) \_\_\_\_\_

A)  $\frac{1}{2} \sqrt{2 - \sqrt{2}}$

B)  $-\frac{1}{2} \sqrt{2 + \sqrt{2}}$

C)  $-\frac{1}{2} \sqrt{2 - \sqrt{2}}$

D)  $\frac{1}{2} \sqrt{2 + \sqrt{2}}$

**Which answer choice is equivalent to the given expression?**

69)  $\cos x \tan x \csc x$  69) \_\_\_\_\_

A) 1

B)  $\cot x$

C)  $\sin x$

D) 2

**Use the fundamental identities and simplify the expression to get a numerical value.**

70)  $\cos x (\csc x - \sec x) - \cot x$  70) \_\_\_\_\_

A) 1

B) -1

C) 0

D)  $\cos^2 x - \tan^2 x$

71)  $\sin^2 x (\cot^2 x + 1)$  71) \_\_\_\_\_

A)  $\tan^2 x$

B) 1

C)  $\cos^2 x + 1$

D) -1

**Which answer choice is equivalent to the given expression?**

72)  $\sin 2x \csc x$  72) \_\_\_\_\_

A)  $2 \cot x$

B)  $2 \tan x$

C)  $2 \cos x$

D)  $2 \sec x$

73)  $\frac{1 + \tan^2 x}{\tan^2 x}$  73) \_\_\_\_\_

A)  $\sin^2 x$

B)  $\sec^2 x$

C)  $\csc^2 x$

D)  $\cos^2 x$

74)  $\cos^2 x - \sin^2 x$  74) \_\_\_\_\_

A)  $3 \tan^2 x$

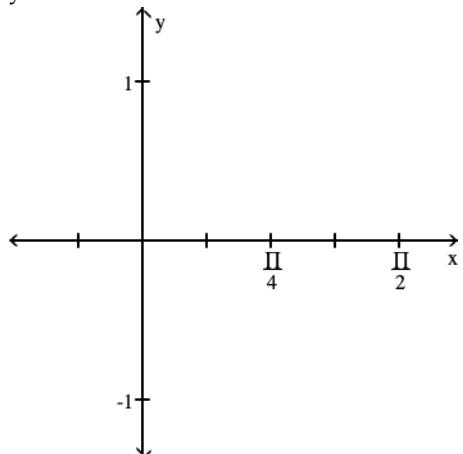
B)  $\csc^2 x$

C)  $2 \cos^2 x - 1$

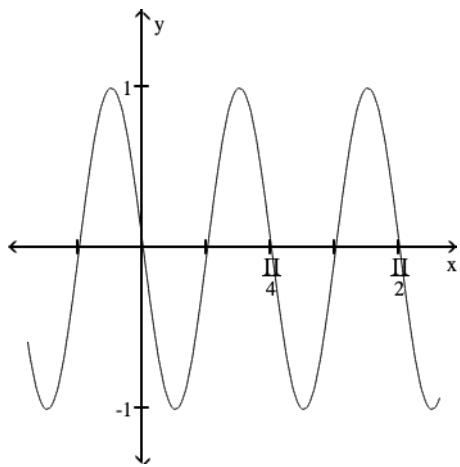
D) 1

**Sketch the graph on the coordinate system provided.**

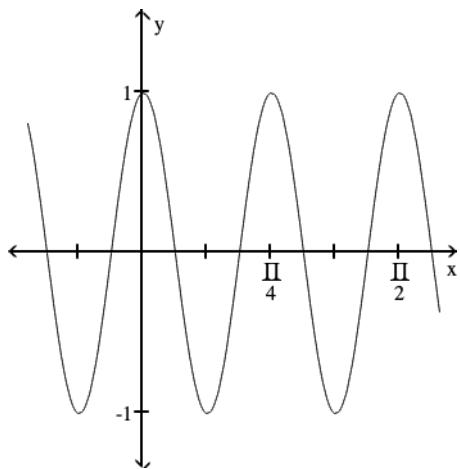
75)  $y = -\sin 8x$



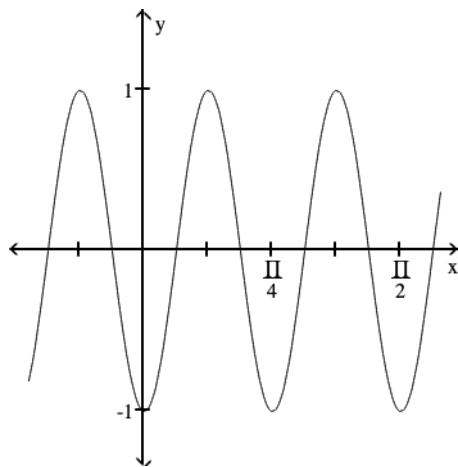
A)



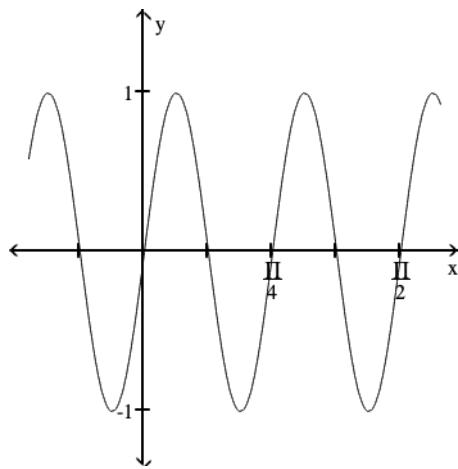
C)



B)

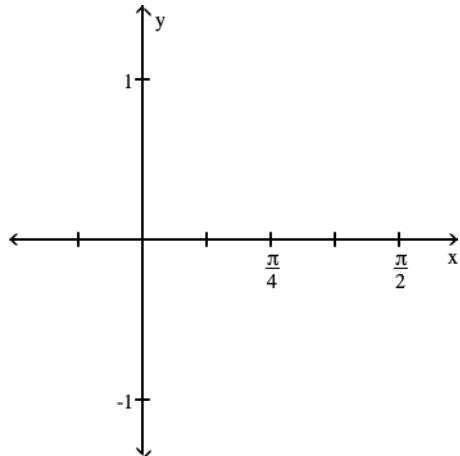
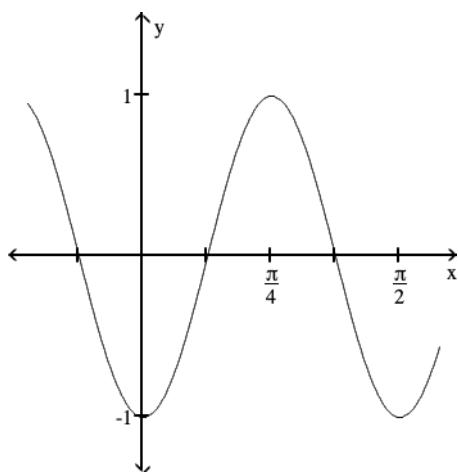
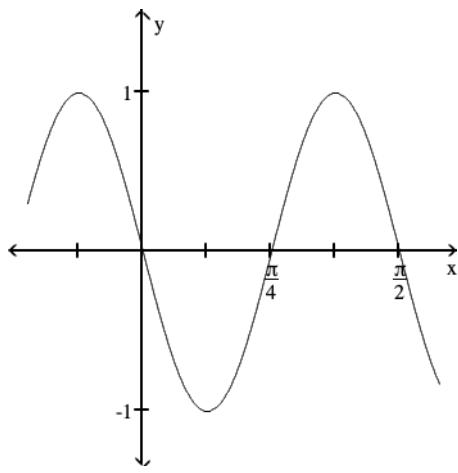


D)

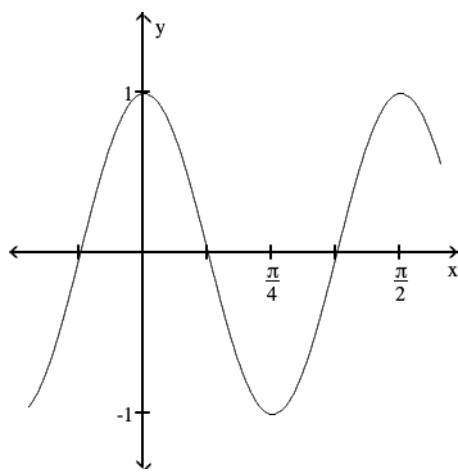
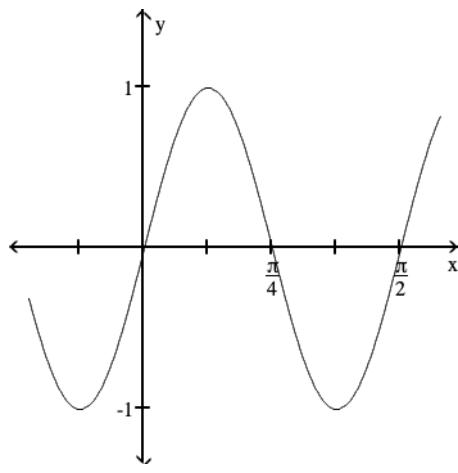


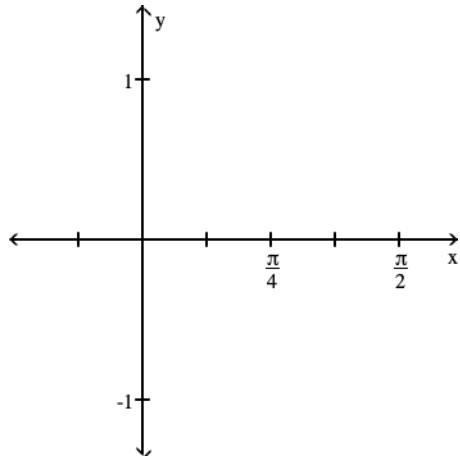
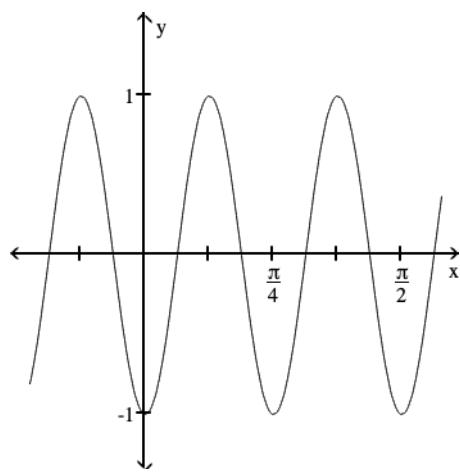
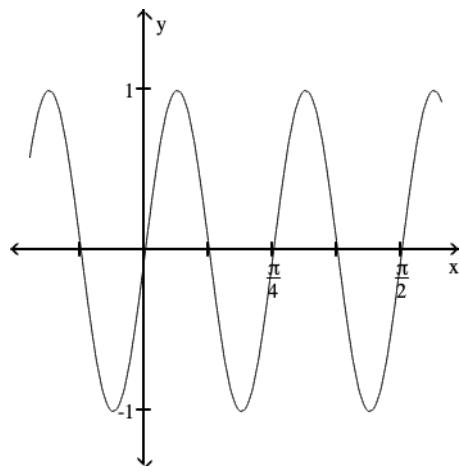
State the period of the function and graph.

75) \_\_\_\_\_

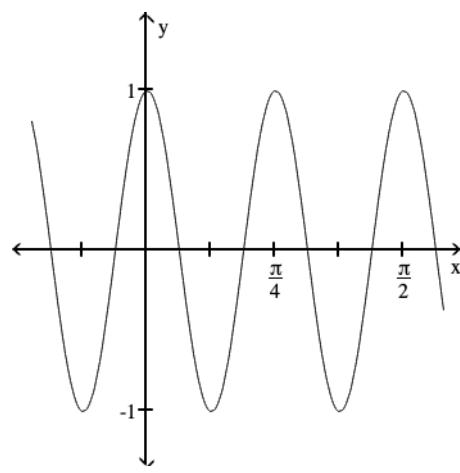
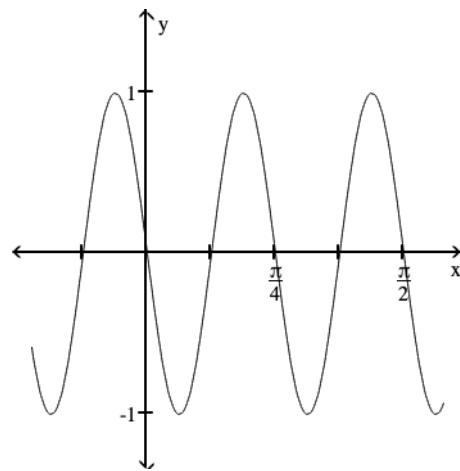
76)  $\sin 4x$ A) Period  $\frac{\pi}{2}$ C) Period  $\frac{\pi}{2}$ 

76) \_\_\_\_\_

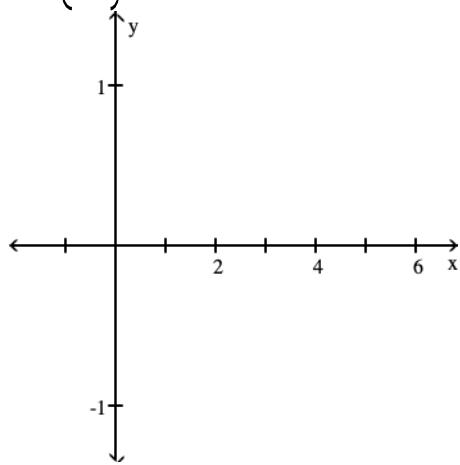
B) Period  $\frac{\pi}{2}$ D) Period  $\frac{\pi}{2}$ 

77)  $\cos 8x$ A) Period  $\frac{\pi}{4}$ C) Period  $\frac{\pi}{4}$ 

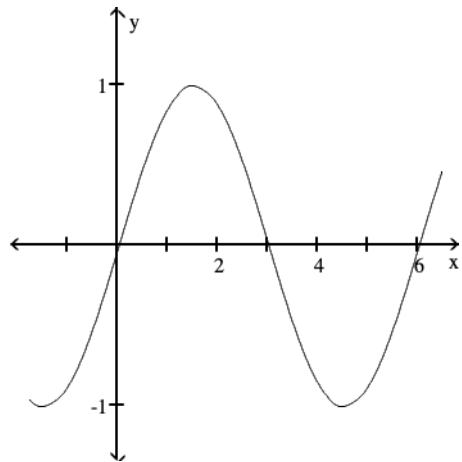
77) \_\_\_\_\_

B) Period  $\frac{\pi}{4}$ D) Period  $\frac{\pi}{4}$ 

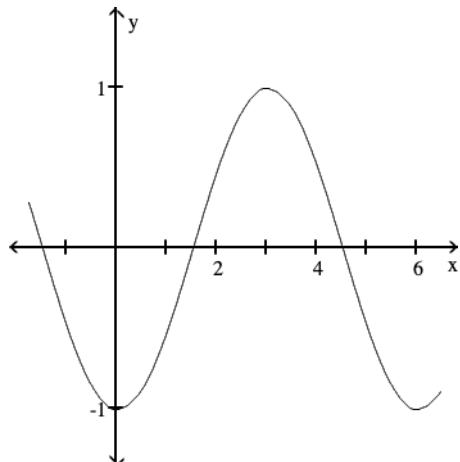
$$78) \sin\left(\frac{\pi x}{3}\right)$$



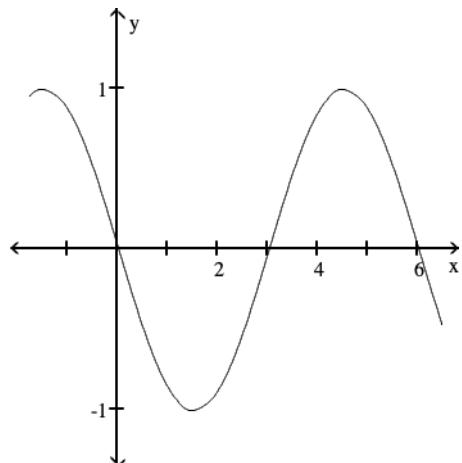
A) Period 6



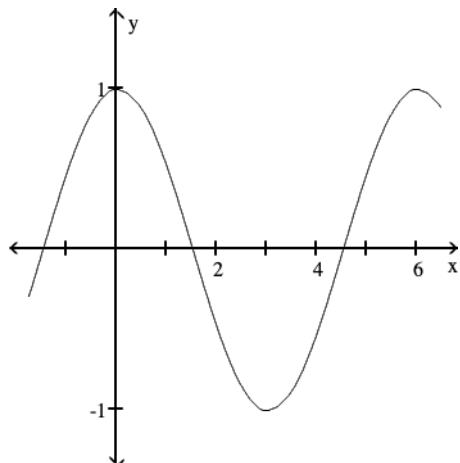
B) Period 6



C) Period 6



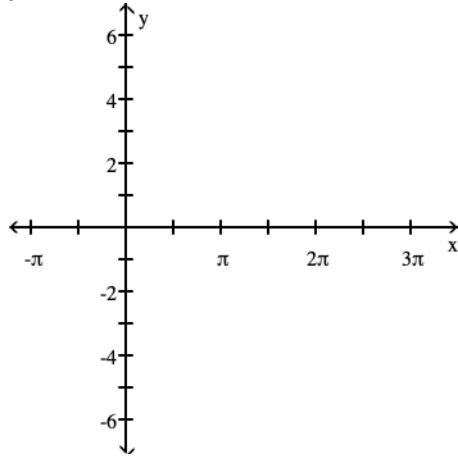
D) Period 6



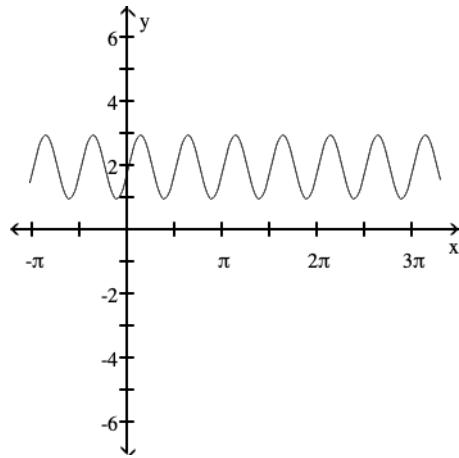
**Graph the function.**

78) \_\_\_\_\_

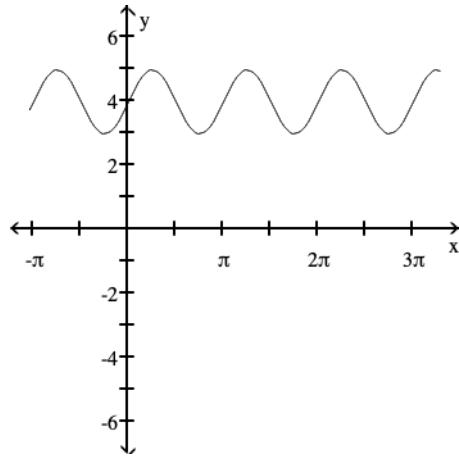
$$79) y = 4 \sin(2x)$$



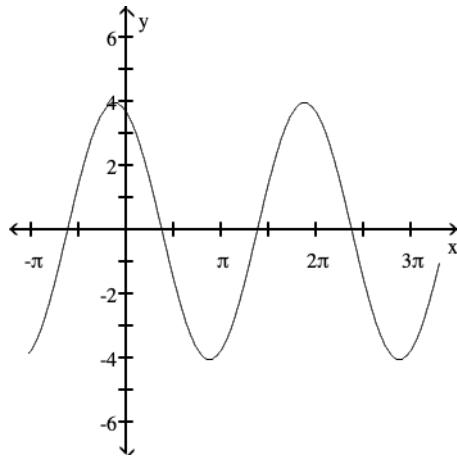
A)



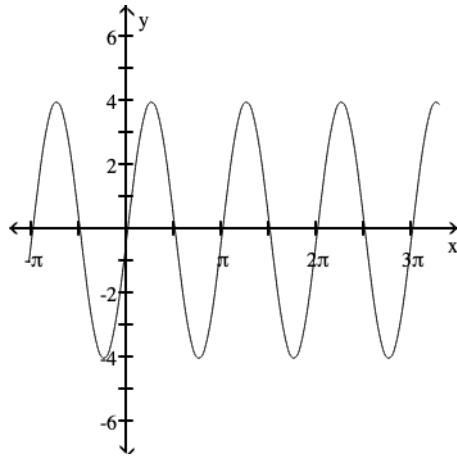
C)



B)



D)

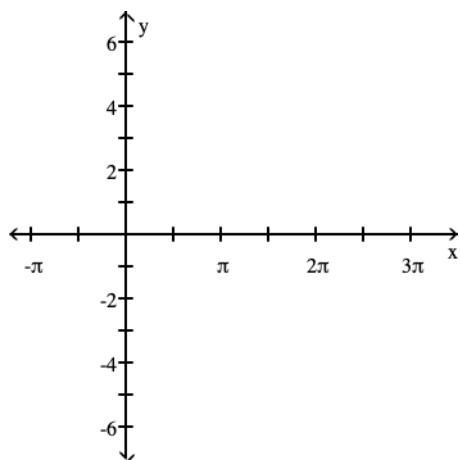


$$79) \underline{\hspace{2cm}}$$

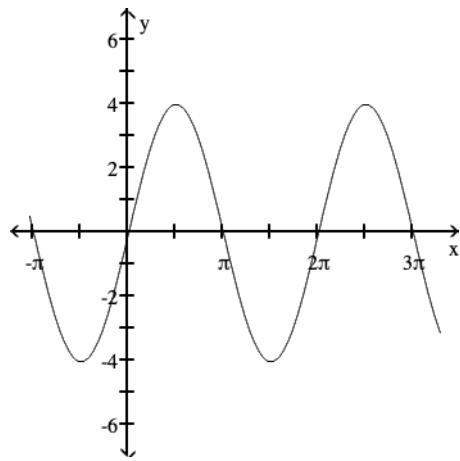
Compute the Amplitud, the Period and sketch the graph of the given equation over a period.

80)  $y = 4 \cos x$

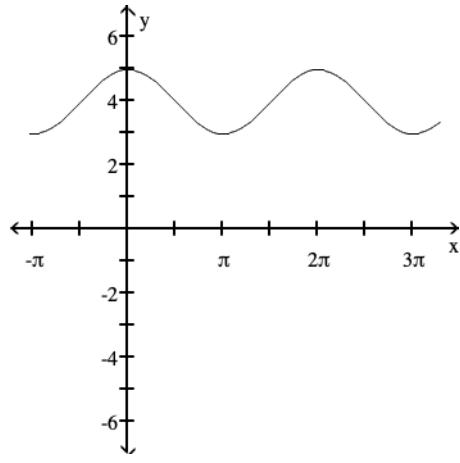
80) \_\_\_\_\_



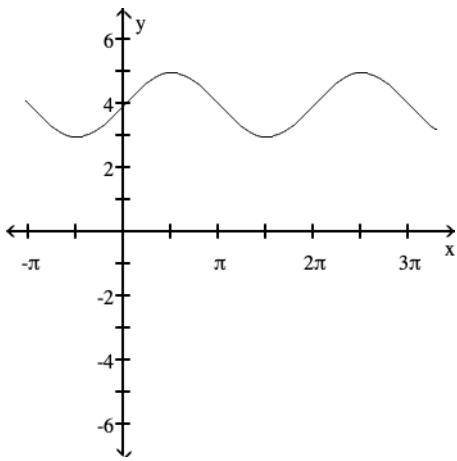
A)



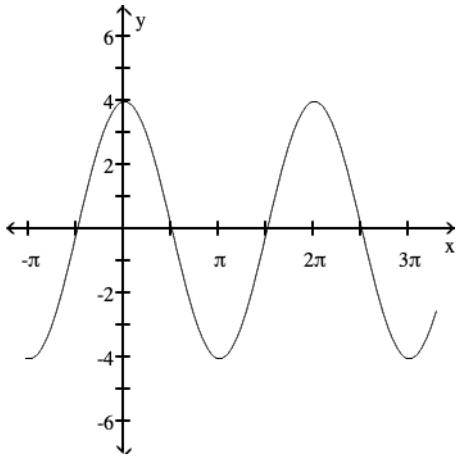
C)



B)



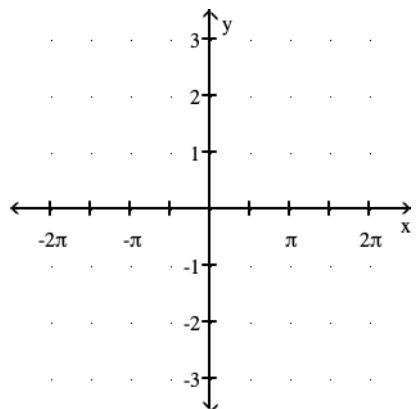
D)



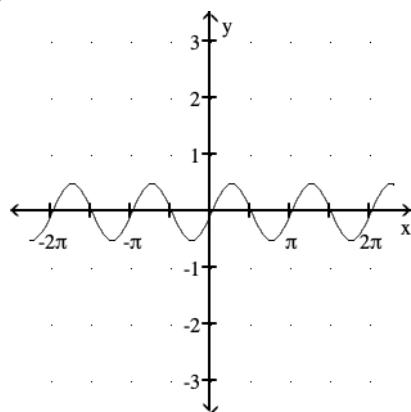
Compute the Amplitud, the Period and sketch the graph of the given equation over a period.

81)  $y = \frac{1}{2} \sin 2x$

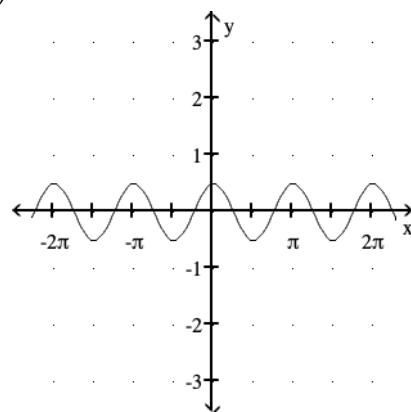
81) \_\_\_\_\_



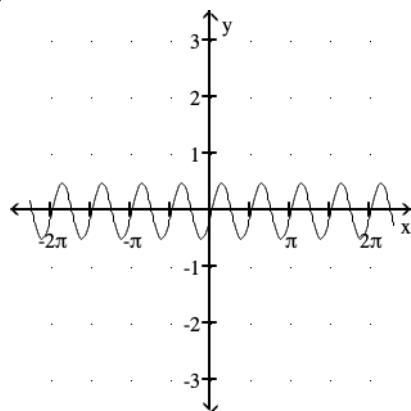
A)



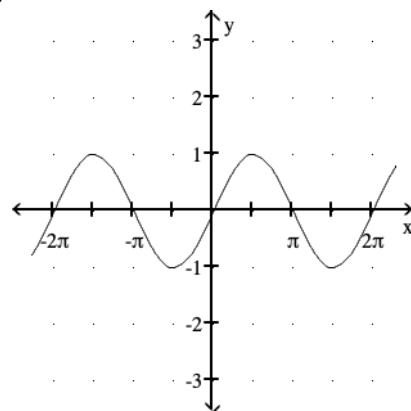
B)



C)

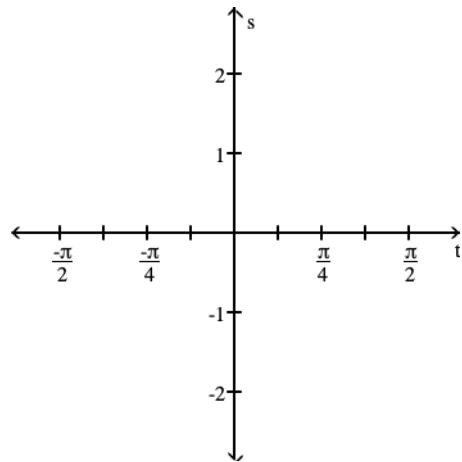


D)

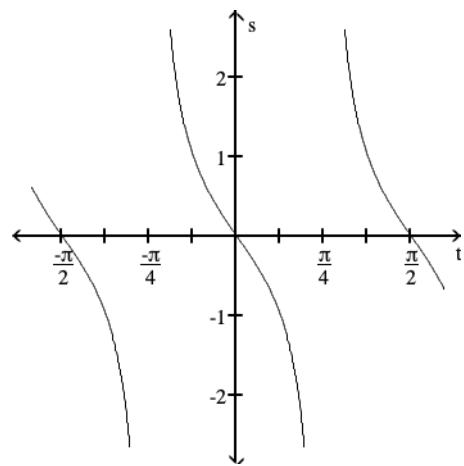


Graph the function in the ts-plane (t-axis horizontal, s-axis vertical). State the period and symmetry of the function.

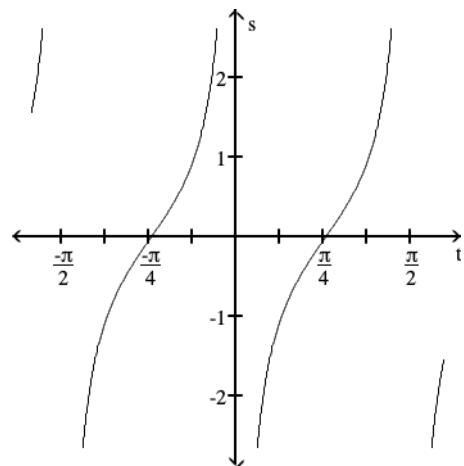
82)  $s = -\tan 2t$



A) Period  $\frac{\pi}{2}$ , symmetric about the origin

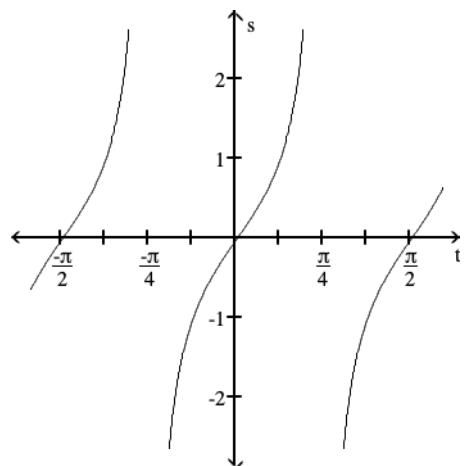


C) Period  $\frac{\pi}{2}$ , symmetric about the origin

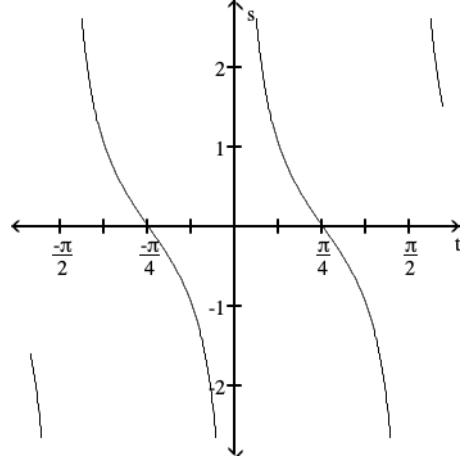


82) \_\_\_\_\_

B) Period  $\frac{\pi}{2}$ , symmetric about the  $s$ -axis



D) Period  $\pi$ , symmetric about the origin



**Use the product-to-sum identities to rewrite the expression as the sum or difference of two functions.**

83)  $\cos 2\theta \cos 6\theta$

83) \_\_\_\_\_

A)  $\frac{1}{2} \cos 8\theta - \frac{1}{2} \cos 4\theta$

B)  $\frac{1}{2} \cos 8\theta - \frac{1}{2} \sin 4\theta$

C)  $\cos^2 8\theta^2$

D)  $\frac{1}{2} \cos 4\theta + \frac{1}{2} \cos 8\theta$

84)  $\sin 3\theta \sin 5\theta$

84) \_\_\_\_\_

A)  $-\frac{1}{2} \cos 2\theta - \frac{1}{2} \cos 8\theta$

B)  $\frac{1}{2} \cos 8\theta - \frac{1}{2} \sin 2\theta$

C)  $\frac{1}{2} \cos 2\theta - \frac{1}{2} \cos 8\theta$

D)  $\sin^2 15\theta^2$

**Use sum-to-product identities to rewrite the expression as a product.**

85)  $\sin \frac{\pi}{11} - \sin \frac{\pi}{2}$

85) \_\_\_\_\_

A)  $2 \sin \frac{13\pi}{44} \cos \frac{9\pi}{44}$

B)  $-2 \sin \frac{9\pi}{44} \sin \frac{13\pi}{44}$

C)  $2 \cos \frac{9\pi}{44} \cos \frac{13\pi}{44}$

D)  $-2 \cos \frac{13\pi}{44} \sin \frac{9\pi}{44}$

86)  $\cos 4x + \cos 2x$

86) \_\_\_\_\_

A)  $2 \cos 3x$

B)  $2 \cos 3x \sin x$

C)  $2 \cos 3x \cos x$

D)  $2 \sin 3x \sin x$

87)  $\sin 8x + \sin 2x$

87) \_\_\_\_\_

A)  $2 \sin 5x \sin 3x$

B)  $2 \cos 5x \sin 3x$

C)  $2 \sin 5x \cos 3x$

D)  $2 \sin 10x$

**Solve the equation on the interval  $0 \leq \theta < 2\pi$ .**

88)  $\cos \theta - 1 = 0$

88) \_\_\_\_\_

A) 0

B)  $\frac{3\pi}{2}$

C)  $\frac{\pi}{2}$

D)  $\pi$

89)  $5 \csc \theta - 1 = 4$

89) \_\_\_\_\_

A)  $\frac{\pi}{2}$

B)  $\pi$

C)  $\frac{3\pi}{2}$

D)  $2\pi$

90)  $2 \cos \theta + 1 = 0$

90) \_\_\_\_\_

A)  $\frac{2\pi}{3}, \frac{4\pi}{3}$

B)  $\frac{\pi}{2}, \frac{3\pi}{2}$

C)  $\frac{\pi}{3}, \frac{5\pi}{3}$

D)  $\frac{3\pi}{2}$

**Solve the equation. Give a general formula for all the solutions.**

91)  $\cos \theta - 1 = 0$

91) \_\_\_\_\_

A)  $\theta = \frac{\pi}{2} + 2k\pi$

B)  $\theta = 2k\pi$

C)  $\theta = \frac{3\pi}{2} + 2k\pi$

D)  $\theta = \pi + 2k\pi$

92)  $\sin \theta = 1$

92) \_\_\_\_\_

A)  $\theta = 0 + 2k\pi$

B)  $\theta = \pi + 2k\pi$

C)  $\theta = \frac{\pi}{2} + 2k\pi$

D)  $\theta = \frac{3\pi}{2} + 2k\pi$

93)  $\sin \theta = \frac{\sqrt{3}}{2}$

93) \_\_\_\_\_

A)  $\theta = \frac{\pi}{6} + k\pi, \theta = \frac{5\pi}{6} + k\pi$

B)  $\theta = \frac{\pi}{6} + 2k\pi, \theta = \frac{5\pi}{6} + 2k\pi$

C)  $\theta = \frac{\pi}{3} + k\pi, \theta = \frac{2\pi}{3} + k\pi$

D)  $\theta = \frac{\pi}{3} + 2k\pi, \theta = \frac{2\pi}{3} + 2k\pi$

94)  $2 \cos \theta + 1 = 0$

94) \_\_\_\_\_

A)  $\theta = \frac{3\pi}{2} + k\pi$

B)  $\theta = \frac{2\pi}{3} + k\pi, \theta = \frac{4\pi}{3} + k\pi$

C)  $\theta = \frac{2\pi}{3} + 2k\pi, \theta = \frac{4\pi}{3} + 2k\pi$

D)  $\theta = \frac{\pi}{2} + 2k\pi, \theta = \frac{3\pi}{2} + 2k\pi$

**Solve for the angle  $\theta$ , where  $0 \leq \theta \leq 2\pi$** 

95)  $\sin^2 \theta = \frac{1}{4}$

95) \_\_\_\_\_

A)  $\theta = 0, \pi, 2\pi$

B)  $\theta = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$

C)  $\theta = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$

D)  $\theta = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$

96)  $\cos^2 \theta = \frac{1}{4}$

96) \_\_\_\_\_

A)  $\theta = 0, \pi, 2\pi$

B)  $\theta = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$

C)  $\theta = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$

D)  $\theta = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$

## Answer Key

Testname: REVIEW FOR FINAL EXAM

- 1) B
- 2) D
- 3) B
- 4) C
- 5) B
- 6) B
- 7) A
- 8) C
- 9) B
- 10) C
- 11) A
- 12) A
- 13) B
- 14) D
- 15) B
- 16) B
- 17) B
- 18) C
- 19) C
- 20) A
- 21) D
- 22) D
- 23) B
- 24) C
- 25) D
- 26) A
- 27) D
- 28) D
- 29) B
- 30) C
- 31) A
- 32) B
- 33) C
- 34) A
- 35) B
- 36) B
- 37) B
- 38) D
- 39) B
- 40) D
- 41) D
- 42) D
- 43) C
- 44) A
- 45) C
- 46) D
- 47) C
- 48) B
- 49) A

## Answer Key

### Testname: REVIEW FOR FINAL EXAM

50) D

51) C

52) B

53) B

54) C

55) A

56) D

57) A

58) D

59) C

60) A

61) D

62) C

63) D

64) B

65) C

66) C

67) C

68) D

69) A

70) B

71) B

72) C

73) C

74) C

75) A

76) D

77) B

78) A

79) D

80) D

81) A

82) A

83) D

84) C

85) D

86) C

87) C

88) A

89) A

90) A

91) B

92) C

93) D

94) C

95) B

96) B